

How well can we predict future epidemics from small scale outbreaks?

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Outline

- Real-world motivation
- Spatio-temporal Model
- Bayesian inference
- Model choice
- Conclusions

Real-world Motivation

- Emerging and re-emerging pathogens
- Analysis of historical outbreaks inform control of future outbreaks
- Data: detection times known
- Data: At risk premises known
- Limited/negligible animal movement
- Infection local: intensity a function of distance
- Control: depopulation of detected premises

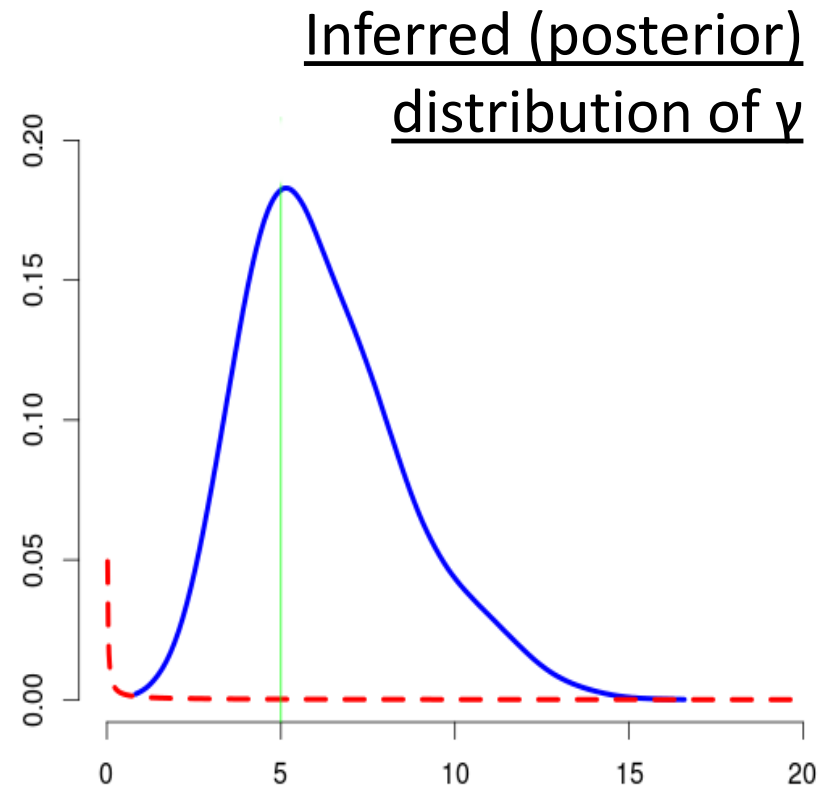
- No knowledge of times of infection
- Example of Classical Swine Fever (CSF) in UK

Homogeneous farms model

- SIR model on closed spatial population, size N
- An individual i makes an infectious contact with a susceptible individual j at rate $\beta_{ij} = \beta_0 h_{ij}$
- β_{ij} : the kernel transmission function
- h_{ij} : the distance kernel
- The infectious period follows: $R_i - I_i \approx Ga(\alpha, \gamma)$
- Data augmentation techniques employed for the unknown infection times. Inference more challenging with small scale epidemics coming from emerging and re-emerging pathogens

Bayesian Inference with MCMC framework

- Enables statistical inference of
 - parameter values
 - **infection times**
- MCMC methods draw successive samples from 'posterior' distribution
- In practice, interests lie in infectious period and kernel transmission functions



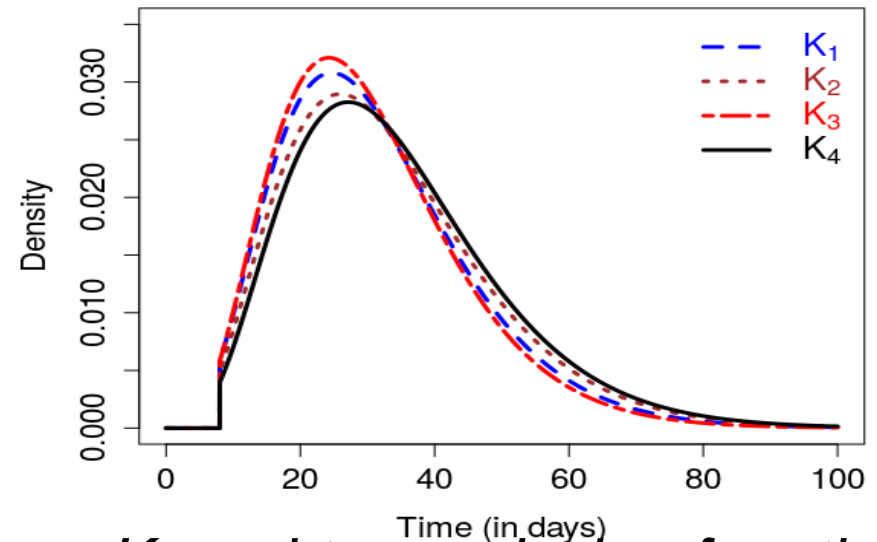
Based on simulated data with true values: $\gamma = 5$, $\alpha = 5$, $\beta_0 = 0.35$,
#premises = 201, #infected sites $n = 43$

CSF in East Anglia Northfolk

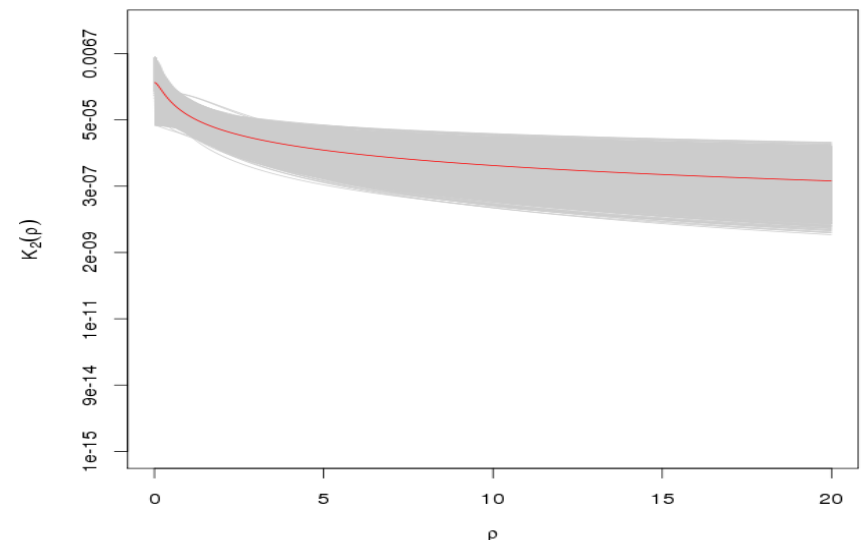
Can apply to real world data even on small outbreaks

- $N = 1703$ farms with exact location or coordinates
- 16 reported cases
- Can fit multiple models e.g. different kernels
- And infer disease characteristics \Rightarrow

Average infectious period

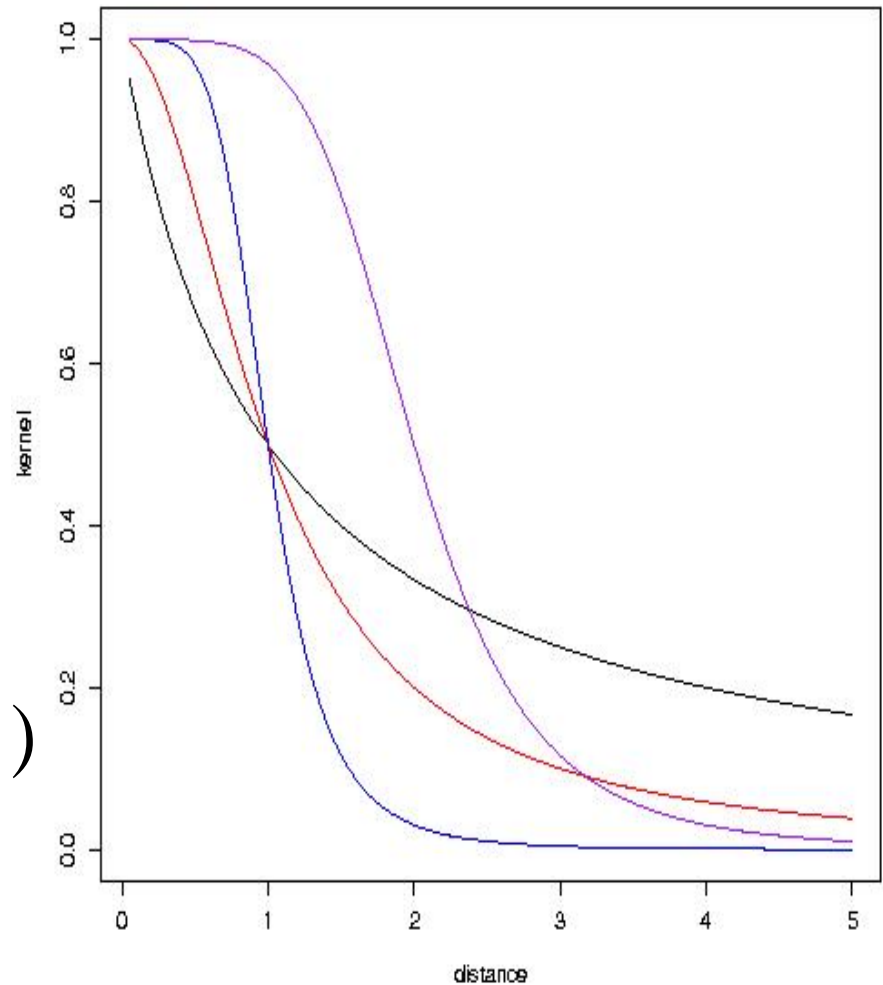


Kernel transmission function

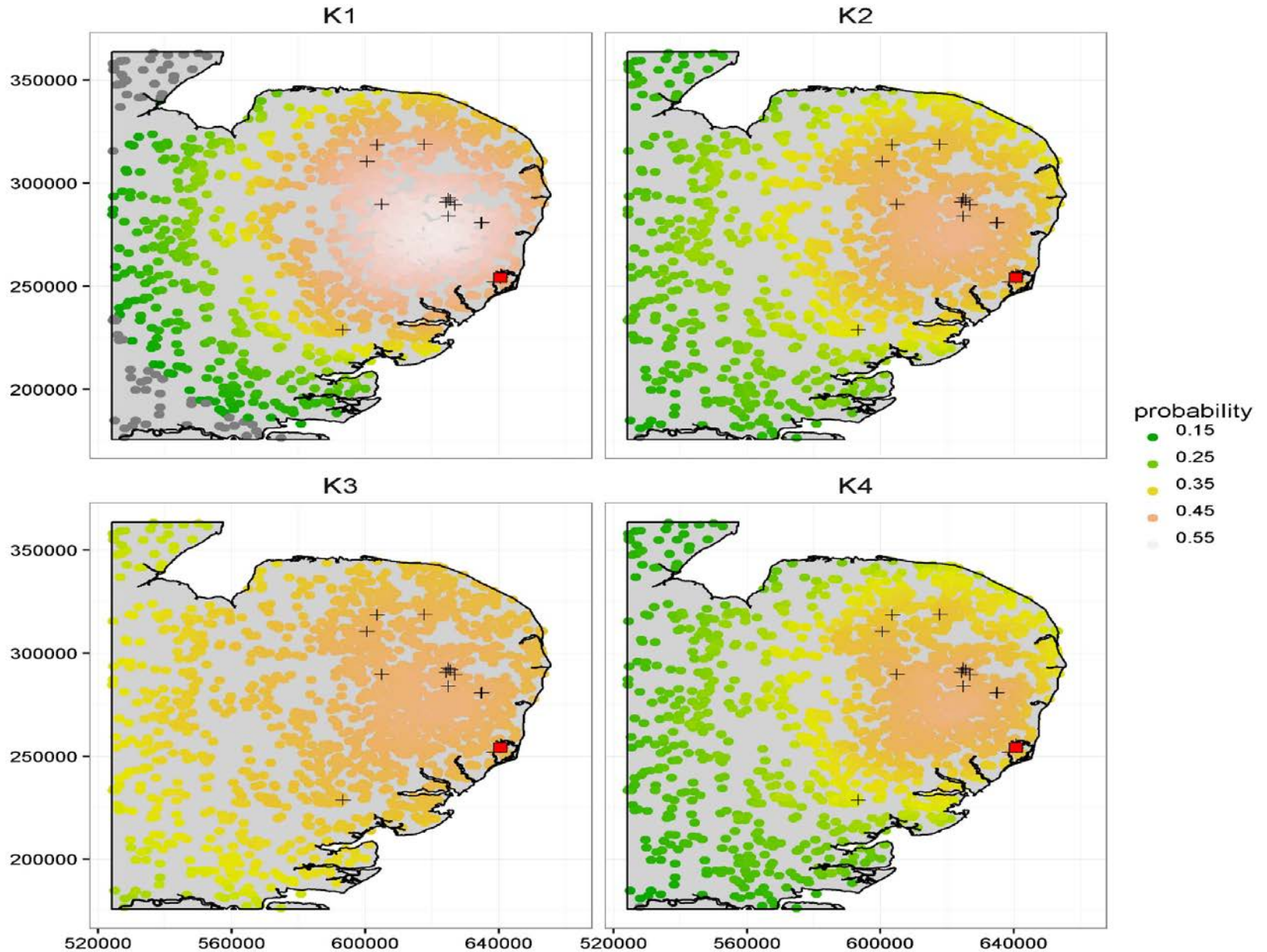


Fit different spatial kernel transmission functions

- K1: $\exp(-\tau\rho(i, j))$
- K2: $\frac{1}{1 + (\rho(i, j) / d)^a}$
- K3: $\frac{1}{1 + (\rho(i, j) / d)}$
- K4: $1 - \exp(-(\rho(i, j) / d)^{-a})$



CSF risk assessment: model dependent



Bayesian model choice tools

- **DIC** is a model comparison criterion measuring trade-off between the fit of the data and the complexity of the model: $DIC = \text{“goodness of fit”} + \text{“complexity”}$

Problems: non invariance to reparameterisation, lack of consistency, weak theoretical justification

- **Bayesian Latent residuals**: unobserved, iid uniform r.v. that conform with the assumed data generation process

Test various components of models and “true” assumptions present uniformly distributed residuals

Discussion

- Inferred kernel transmission functions for CSF
- Applied novel model selection tools to assess and select kernels

- Assessing the amount of data needed for correct kernel identification in real-time epidemic outbreaks
- Account for socio-economic effects in modelling epidemics
- Make the models more dynamic by accounting for control strategies at different points in time

Reference

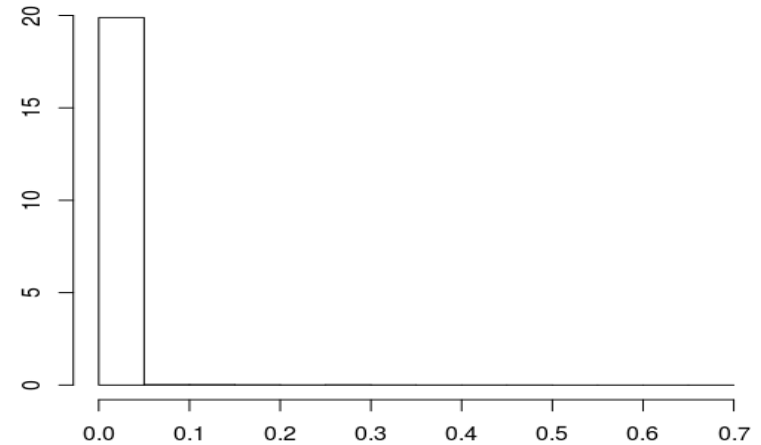
K Gamado, G Marion & T Porphyre. Data-Driven Risk Assessment from Small Scale Epidemics: Estimation and Model Choice for Spatio-Temporal Data with Application to a Classical Swine Fever Outbreak. *Frontiers in Veterinary Science* (2017) 4:16

Thanks!

Summary of work on heterogeneity

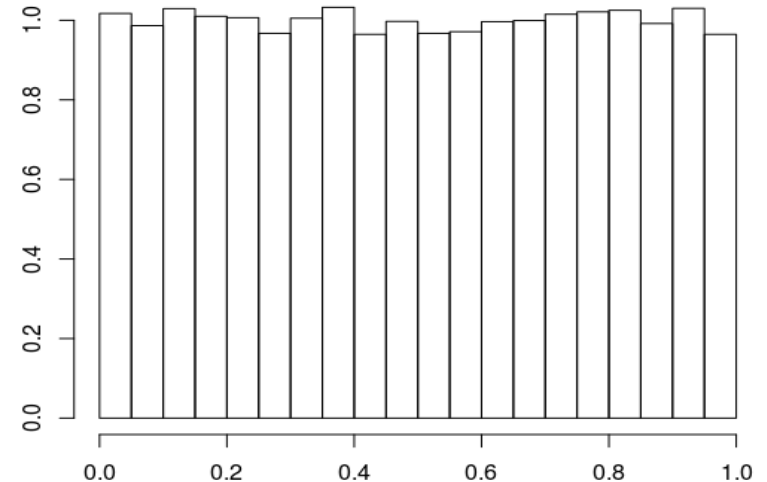
- Groups of detection
- Hierarchy or random effects on removal rates

Homogeneous assumption

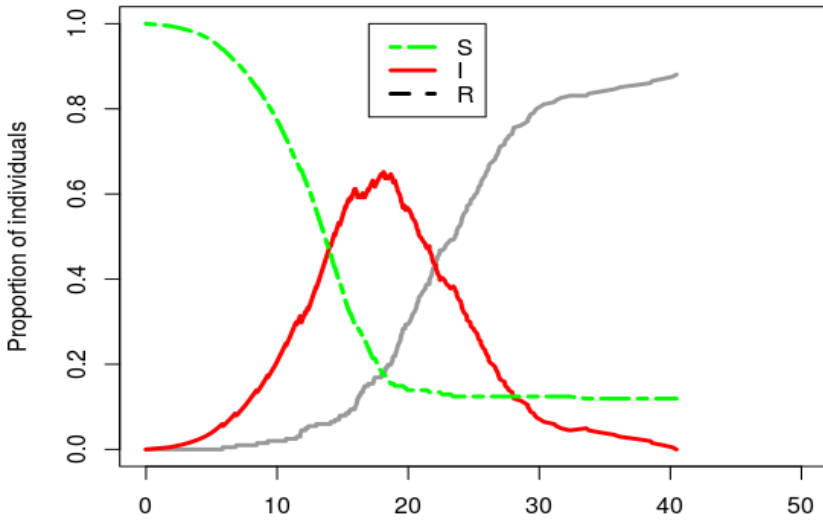


- Groups of susceptibility
- Hierarchy on susceptibility

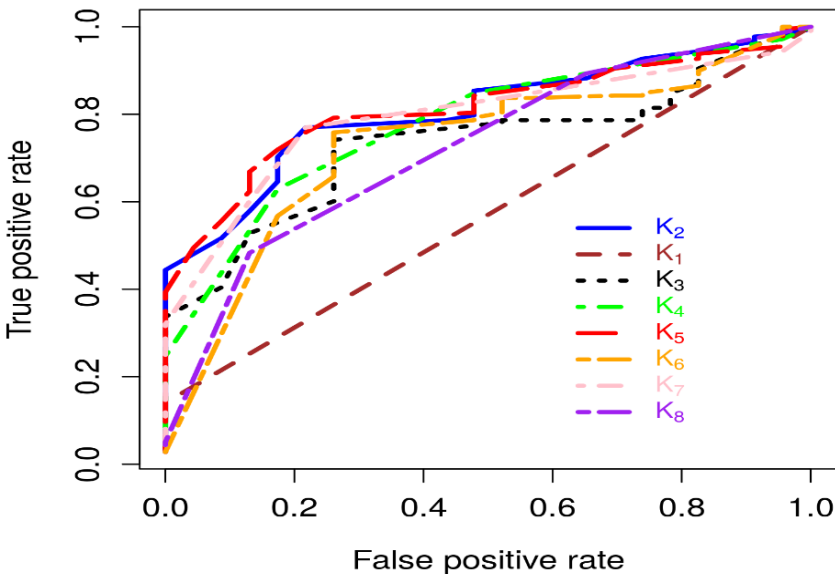
Heterogeneous assumption



Ongoing epidemics example

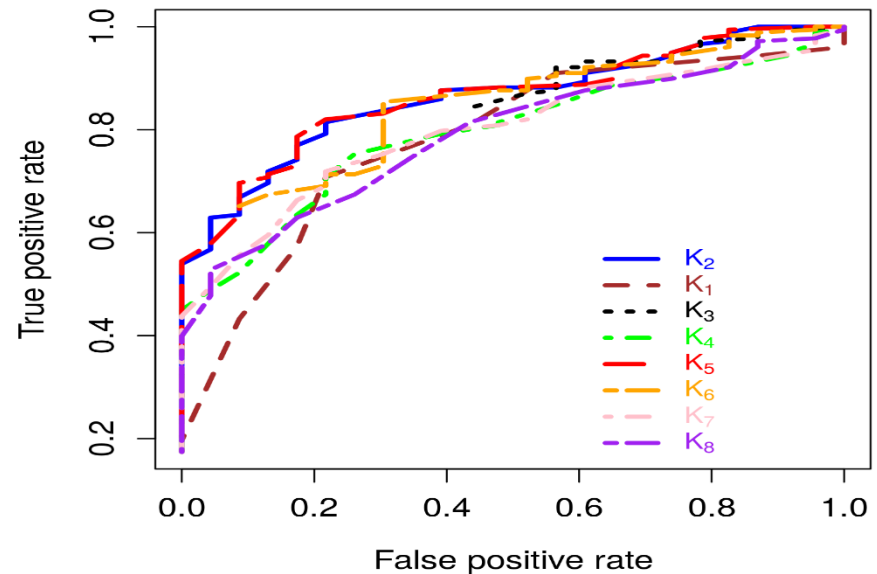


ROC time 11



Observe the epidemic daily
Estimate parameters & LV
prediction of the future
ROC curve

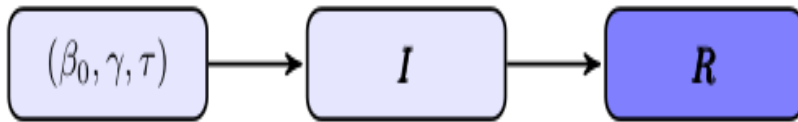
ROC time 17



Computationally efficient inference

Centered and non-centered schemes

- Standard algorithms adopt a 'centred' approach.

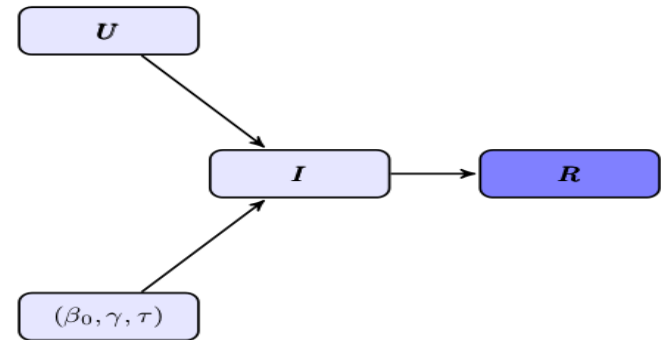


- updating the model parameters
- then updating the latent or unobserved variables

- Non-centering scheme

$$U_i = \gamma(R_i - I_i)$$

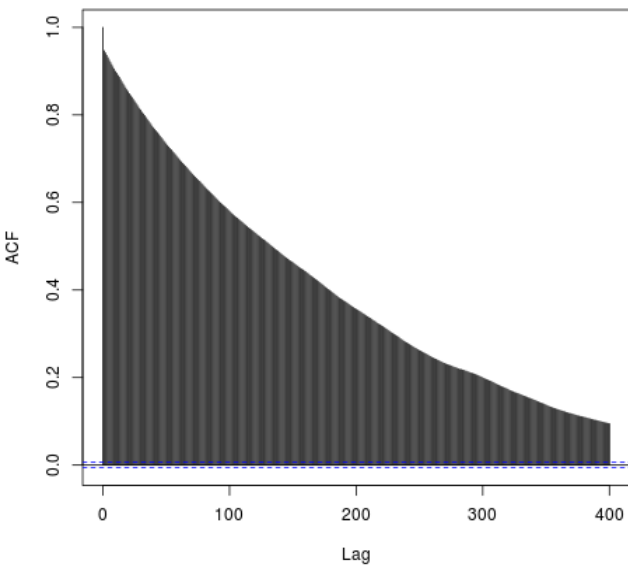
$$(I, \beta_0, \gamma, \alpha, R) \rightarrow (U, \beta_0, \gamma, \alpha, R)$$



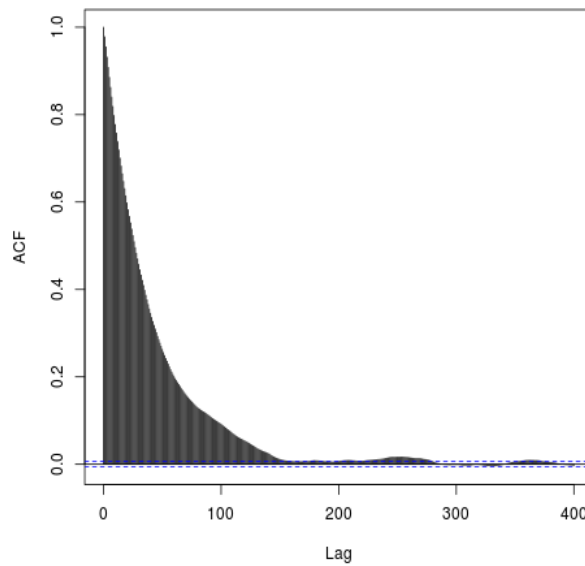
- Update simultaneously parameters and latent variables

Non-centred and hybrid schemes are valuable improvement over standard scheme

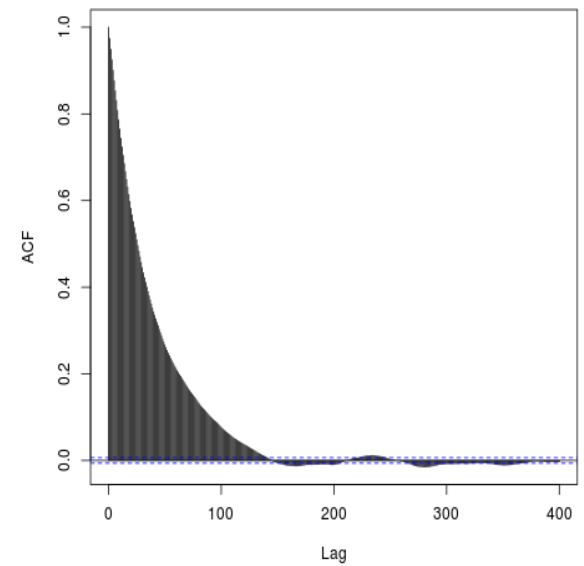
Standard scheme



Non-centred scheme



Hybrid scheme



Non centred parameterisation enables

- correlated moves in Markov chain
- more efficient exploration of posterior
- faster MCMC for complex models
- Non-centered & hybrid schemes reduce autocorrelation

Variability between farms

- ❖ Most models assume homogeneity of farms
- ❖ In reality, each farm is likely to behave differently depending on farm type
- ❖ Bio-security practices, areas of location, reaction to epidemic...
- ❖ Generally one aim of our research is to move away from the assumptions of constant susceptibility, infectivity and detection, all to be functions of farms' characteristics

Examples of heterogeneity

- Different detection rates per group

Assume there are n groups of farms: G_1 to G_n

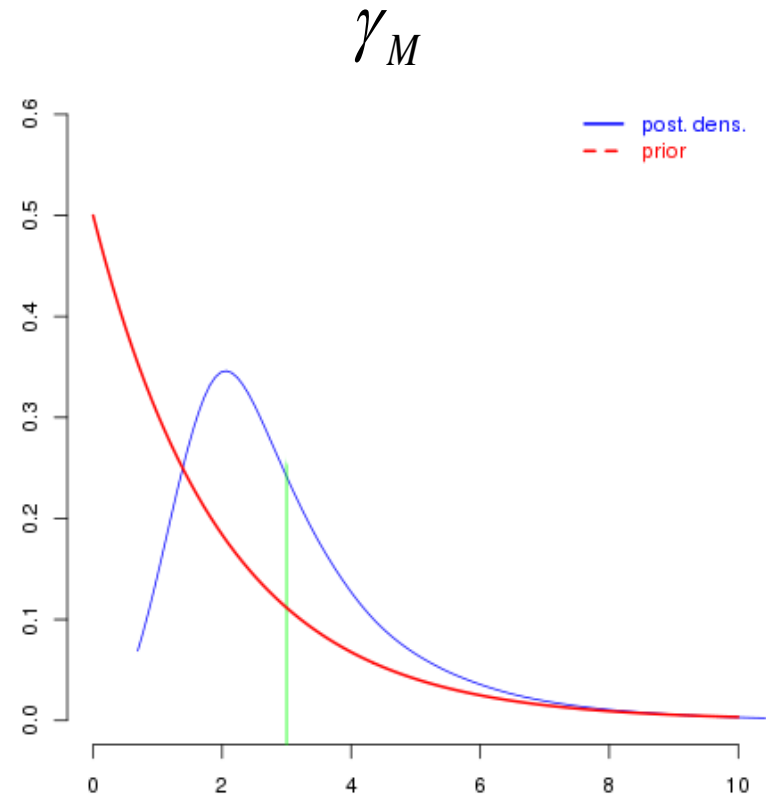
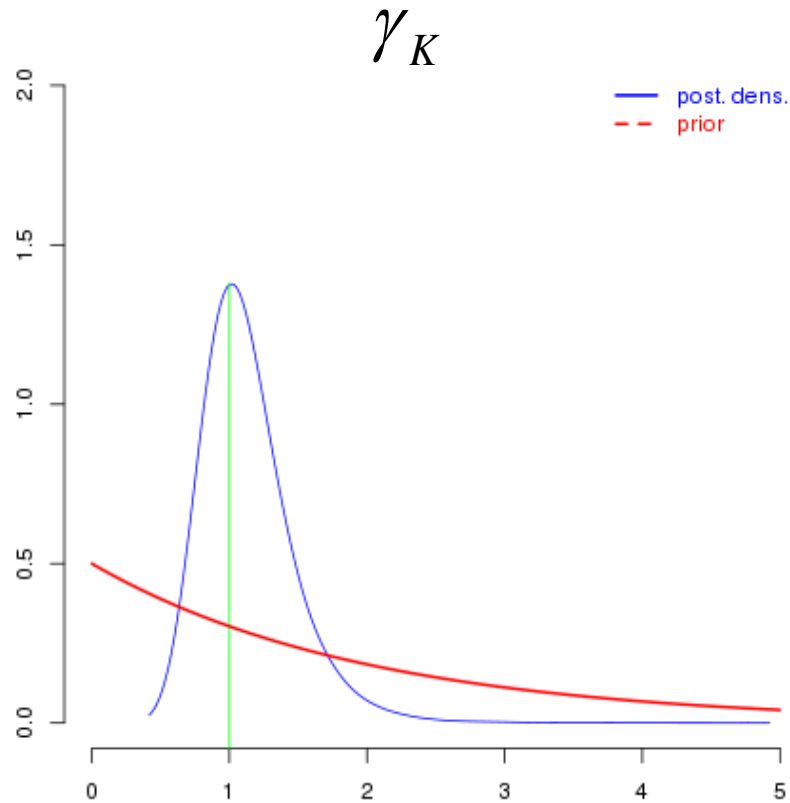
The infectious period follows: $R_i - I_i \approx Ga(\alpha, \gamma_s)$

$$s \in G_s$$

- Different groups of susceptibility

Kernel transmission function: $\beta_0^s h_{ij}$

Inferring the rates per group



- The data consist of the detection times of the infected premises and the groups of each farm
- LR helps to select models with heterogeneity when it is the “truth”